# Séminaire de Mathématiques et Informatique

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## Existence, uniqueness and stability of solutions for systems of differential equations involving $\psi$ -fractional derivatives of arbitrary order.

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#### Abstract

We present results on the existence and uniqueness of solutions for systems of differential equations with boundary conditions involving fractional intergrals and derivatives of a function with respect to another one. Our main tool is fixed-point theory. We also study the stability of those systems according to the Ulam-Hyers stability. Finally, we provide some numerical illustrative examples.

#### Mathematics Subject Classification: 26A33, 34B18, 34B27

**Keywords:** Fractional integral and derivative, fixed-point theory, existence and uniqueness, Ulam-Hyers stability.

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